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## ON THE CONFUSION OF PLANCK FEEDBACK PARAMETERS

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### ABSTRACT

The Planck feedback parameter  $\lambda_0$  is the most fundamental quantity in the theory of global warming, because the surface temperature change  $\Delta T_{s,0}$  is calculated by—(radiative forcing due to CO<sub>2</sub> doubling)/ $\lambda_0$  in the absence of feedbacks other than that of surface temperature change. The following three groups of Planck feedback parameters are found in the literature depending on the choice of temperature  $T_s$  and the outgoing long wave radiation (OLR) at the top of atmosphere in equation of  $\lambda_0 = -4\text{OLR}/T_s$ , which is derived from the Stefan-Boltzmann Law.

GROUP A:  $T_s = 288\text{K}$  and  $\text{OLR} = 231\text{--}243\text{W/m}^2$      $\lambda_0 = -3.21 \text{--} -3.37(\text{W/m}^2)/\text{K}$

GROUP B:  $T_s = 255\text{K}$  and  $\text{OLR} = 242\text{W/m}^2$ ,     $\lambda_0 = -3.8(\text{W/m}^2)/\text{K}$

GROUP C:  $T_s = 288\text{K}$  and  $\text{OLR} = 492\text{--}514\text{W/m}^2$      $\lambda_0 = -6.8 \text{--} -7.1(\text{W/m}^2)/\text{K}$

This study shows that  $\lambda_0$  of GROUP C is a theoretically relevant choice for  $T_s$  and OLR, rather than those of GROUP A and GROUP B, while the IPCC adopted  $\lambda_0$  of GROUP A. Although the surface temperature change  $\Delta T_s$  is 3.0K with  $\lambda_0 = -3.21(\text{W/m}^2)/\text{K}$  for CO<sub>2</sub> doubling when lapse rate, water vapor, surface albedo and cloud feedbacks are included in the IPCC AR4, it is shown to be 0.5–0.75K with  $\lambda_0 = -6.8(\text{W/m}^2)/\text{K}$  in the present study.

Since the IPCC overestimates the threat of carbon dioxide by 4–6 times, the reevaluation will be needed for the CO<sub>2</sub> reduction policies in terms of cost and potential hazards.

### 1. INTRODUCTION

Climate sensitivity  $\Delta T_s$  indicates the change in the global mean surface temperature  $T_s$  when the concentration of atmospheric CO<sub>2</sub> is doubled from the pre-industrial level of 280 ppm to 560 ppm. It is expressed as the product of the climate sensitivity parameter  $\Lambda$  and the radiative forcing due to CO<sub>2</sub> doubling  $\Delta Q$ , namely  $\Delta T_s = \Lambda \times \Delta Q$  [Cess et al., 1990].

The climate system reacts to this external forcing through the various feedback processes, such as the change in surface temperature, lapse rate, water vapor concentration, surface albedo, as well as the cloud amount and its properties [Bony et al.,

2006; Soden et al., 2006]. Therefore, two types of climate sensitivity and their corresponding parameters can be defined as follows.

- (a) Climate sensitivity  $\Delta T_{s,0}$  and climate sensitivity parameter  $\Lambda_0$  without feedbacks other than change in surface temperature, which is called Planck feedback.
- (b) Climate sensitivity  $\Delta T_s$  and climate sensitivity parameter  $\Lambda$  with the feedbacks of surface temperature, lapse rate, water vapor, surface albedo and cloud.

Schlesinger proposed a linear model of the climate system as follows [Schlesinger, 1986].

$$N = N(E_i, T_s, I_j) \text{ and } I_j = I_j(T_s) \quad (1)$$

Then,

$$\Delta N = \partial N / \partial E_i \times \Delta E_i + \partial N / \partial T_s \times \Delta T_s + \partial N / \partial I_j \times dI_j / dT_s \times \Delta T_s \quad (2)$$

Here in the formula,

$N$ : the net energy flux at the top of atmosphere (TOA) The sign of flux is plus when the flux is downward.

$E_i$ : the vector of external variables to the climate system such as atmospheric  $\text{CO}_2$  concentration.

$I_j$ : the vector of internal variables in the climate system other than  $T_s$  such as lapse rate, water vapor concentration, surface albedo, cloud amount and its properties.

$\Delta Q$ : the external forcing defined as  $\Delta Q = \partial N / \partial E_i \times \Delta E_i$

$\lambda_0$ : the Planck feedback parameter defined as  $\lambda_0 = \partial N / \partial T_s$

$\lambda_j$ : the feedback parameter of internal variable  $j$  defined as  $\lambda_j = \partial N / \partial I_j \times dI_j / dT_s$

Since  $\Delta N$  is 0 when equilibrium is reached in response to the external forcing  $\Delta Q$ , the change in global mean surface temperature  $\Delta T_s$  can be expressed as follows [Bony et al., 2006].

$$\Delta T_s = -\Delta Q / (\lambda_0 + \lambda_{LR} + \lambda_{WV} + \lambda_A + \lambda_C) = -\Delta Q / \lambda = \Lambda \times \Delta Q \quad (3)$$

Here,  $\lambda = \lambda_0 + \lambda_{LR} + \lambda_{WV} + \lambda_A + \lambda_C$

$\lambda_{LR}$ : lapse rate feedback parameter

$\lambda_{WV}$ : water vapor feedback parameter

$\lambda_A$ : surface albedo feedback parameter

$\lambda_C$ : cloud feedbacks parameter

From Eq. (3), with  $\lambda_j = 0$ , climate sensitivity  $\Delta T_{s,0}$  is expressed as follows in the absence of feedbacks other than the change in surface temperature [Bony et al., 2006].

$$\Delta T_{s,0} = -\Delta Q / \lambda_0 = \Lambda_0 \times \Delta Q \quad (4)$$

Furthermore, the following equations are derived from the above equations [Bony et al., 2006].

$$\Lambda = -1/\lambda \quad \text{and} \quad \Lambda_0 = -1/\lambda_0 \quad (5)$$

$$\Delta T_s = \Delta T_{s,0} \times \lambda_0/\lambda = \Delta T_{s,0} \times 1/(1 - g_{LR} - g_{WV} - g_A - g_C) \quad (6)$$

Here,  $g_{LR}$ : lapse rate feedback gain  $-\lambda_{LR}/\lambda_0$   
 $g_{WV}$ : water vapor feedback gain  $-\lambda_{WV}/\lambda_0$   
 $g_A$ : surface albedo feedback gain  $-\lambda_A/\lambda_0$   
 $g_C$ : cloud feedbacks gain  $-\lambda_C/\lambda_0$

In calculating the climate sensitivity  $\Delta T_s$ , the Planck feedback parameter  $\lambda_0$  is the most fundamental and influential, because it determines  $\Delta T_{s,0}$ , as well as the feedback gains. The sign of  $\lambda_0$  is negative for the negative Planck feedback [Bony et al., 2006; Soden, et al., 2006], although the opposite sign is utilized in some literature [Wetherald et al., 1988].

## 2. $\lambda_0$ DEDUCED FROM MODEL STUDIES

Manabe et al., reported  $\Delta T_{s,0} = 1.3\text{K}$  for  $\text{CO}_2$  doubling utilizing a radiative-convective model (RCM) with a fixed critical lapse rate of  $6.5 \text{ K/km}$  for convective adjustment, fixed absolute humidity, fixed cloud altitude, fixed cloud cover, fixed cloud optical depth and fixed surface albedo [Manabe et al., 1964; Manabe et al., 1967]. Although the radiative forcing due to  $\text{CO}_2$  doubling  $\Delta Q$  is not shown in their paper, it can be estimated as  $3.5 \text{ W/m}^2$  from the general circulation model (GCM) study incorporating the same RCM [Manabe et al., 1975], which yields  $\lambda_0 = -2.7 \text{ (W/m}^2\text{)/K}$ .

Hansen et al., obtained  $\Delta T_{s,0} = 1.2\text{K}$  utilizing an RCM with the same characteristics as that of Manabe et al., with  $\Delta Q = 4.0 \text{ W/m}^2$  [Hansen et al., 1981], which corresponds to  $\lambda_0 = -3.3 \text{ (W/m}^2\text{)/K}$ .

Schlesinger also conducted an RCM study showing  $\Delta T_{s,0} = 1.3\text{K}$  with  $\Delta Q = 4.0 \text{ W/m}^2$  to obtain a climate sensitivity parameter  $\Lambda_0$  of  $0.3 \text{ K/(W/m}^2\text{)}$  [Schlesinger, 1986], which means that  $\lambda_0 = -3.3 \text{ (W/m}^2\text{)/K}$ .

Although the above three RCM studies show that  $\lambda_0$  is around  $-3 \text{ (W/m}^2\text{)/K}$ , the computation results of an RCM strongly depend on the various parameterizations such as critical lapse rate for convective adjustment, cloud layer, cloud height, cloud temperature and cloud optical depth [Schneider, 1975; Hummel et al., 1981; Lindzen et al., 1982; Somerville et al., 1984; Schlesinger, 1986]. For instance, Hummel et al., obtained a 25 – 60% smaller surface temperature change  $\Delta T_s$  utilizing a moist adiabatic lapse rate than the  $\Delta T_s$  with the constant  $6.5 \text{ K/km}$  lapse rate used in the above three RCM studies. This will reduce  $\lambda_0$  from  $-3 \text{ (W/m}^2\text{)/K}$  to  $-4 \text{ (W/m}^2\text{)/K}$  –  $-7.5 \text{ (W/m}^2\text{)/K}$  when the same degree of reduction is applied for  $\Delta T_{s,0}$ .

Ramanathan et al., pointed out that a constant  $6.5 \text{ K/km}$  lapse rate is too large for the lower troposphere in his investigations of the actual behavior of the lapse rate at that height [Ramanathan et al., 1978], implying that the moist adiabatic lapse rate is the more realistic parameterization than the constant  $6.5 \text{ K/km}$  lapse rate. In conclusion, an RCM study cannot furnish a Planck feedback parameter  $\lambda_0$  which can serve as the theoretical basis of atmospheric science.

### 3. $\lambda_0$ CALCULATED WITH THE STEFAN-BOLTZMANN LAW

Eq. (7) expresses the radiation budget  $N$  of the earth at the top of the atmosphere (TOA), utilizing the solar constant  $S_0$ , the albedo of the earth  $\alpha$  and the outgoing long wave radiation OLR [Bony et al., 2006].

$$N = (S_0/4)(1 - \alpha) - \text{OLR} \quad (7)$$

Therefore, the Planck feedback parameter  $\lambda_0$  can be calculated by Eq. (8).

$$\lambda_0 = \partial N / \partial T_s = -\partial \text{OLR} / \partial T_s \quad (8)$$

Based on experimental data for OLR as a function of surface temperature and surface albedo measured by satellites, Cess expressed OLR with the modified Stefan-Boltzmann equation as follows [Cess, 1976].

$$\text{OLR} = \epsilon_{\text{eff}} \sigma T_s^{**4} \quad (9)$$

Here,  $\epsilon_{\text{eff}}$ : the effective emissivity of the surface-atmosphere system  
 $\sigma$ : the Stefan-Boltzmann constant

From Eq. (9),  $\lambda_0$  was obtained by differentiation as follows with the assumption that  $\epsilon_{\text{eff}}$  is a constant [Cess, 1976].

$$\lambda_0 = -\partial \text{OLR} / \partial T_s = -4 \epsilon_{\text{eff}} \sigma T_s^{**3} = -4 \text{OLR} / T_s \quad (10)$$

In the Eq. (9), Cess took  $T_s = 288\text{K}$  and  $\epsilon_{\text{eff}} = 0.6$  to obtain  $\text{OLR} = 233 \text{ (W/m}^2\text{)}$ , which gives the following  $\lambda_0$  and  $\Lambda_0$  [Cess, 1976].

$$\lambda_0 = -4 \text{OLR} / T_s = -4 \times 233 / 288 = -3.3 \text{ (W/m}^2\text{)/K} \quad \Lambda_0 = 1 / 3.3 = 0.3 \text{ K/(W/m}^2\text{)}$$

Cess et al., reconfirmed the calculation with  $T_s = 288\text{K}$  and  $\text{OLR} = 240 \text{ W/m}^2$  [Cess et al., 1990]. Wetherald et al., and Tsushima et al., followed Cess's procedures to obtain substantially equivalent results [Wetherald et al., 1988; Tsushima et al., 2005].

The above four studies furnish  $\Delta T_{s,0} = 1.2\text{K}$  utilizing  $4 \text{ W/m}^2$  for the radiative forcing due to  $\text{CO}_2$  doubling [Hansen et al., 1981]. Since this is revised to  $3.7 \text{ W/m}^2$  in the IPCC TAR, the Planck feedback parameter  $\lambda_0$  is changed slightly from  $-3.3 \text{ (W/m}^2\text{)/K}$  to  $-3.21 \text{ (W/m}^2\text{)/K}$  in the 14 GCMs studied for the IPCC AR4 in order to guarantee that  $\Delta T_{s,0} = 1.2\text{K}$  [Soden et al., 2006].

Bony et al., pointed out that the combination of  $T_s = 288\text{K}$  and  $\text{OLR} = 233\text{--}243 \text{ W/m}^2$  did not coincide with the Stefan-Boltzmann Law. They proposed that  $T_s = 255\text{K}$  and  $\lambda_0 = -3.8 \text{ (W/m}^2\text{)/K}$ , which means that  $\text{OLR} = 242 \text{ W/m}^2$  [Bony et al., 2006]. However,  $T_s$  should be  $288\text{K}$  based on the definition of  $\lambda_0$  as shown in Eq. (2) and (8). Therefore, their proposed values failed when tested mathematically.

Schlesinger calculated the climate sensitivity  $\Lambda_0$  using Eq. (11) with  $T_s = 288\text{K}$ , solar constant  $S_0 = 1370 \text{ W/m}^2$  and surface albedo  $\alpha = 0.3$  obtaining  $\Lambda_0 = 0.3 \text{ K/(W/m}^2\text{)}$ , which corresponds to  $\lambda_0 = -3.3 \text{ (W/m}^2\text{)/K}$  [Schlesinger, 1986].

$$\Lambda_0 = T_s / (1 - \alpha) S_0 \quad (11)$$

Equation (11) is derived from Eq. (7), (9) and (10) as follows.  
 From Eq. (7) and (9), the following equation is obtained.

$$N = (S_0/4) (1 - \alpha) - \epsilon_{\text{eff}}\sigma T_s^{**4} \tag{12}$$

At equilibrium, the following equation is obtained, since N is 0.

$$\epsilon_{\text{eff}}\sigma T_s^{**4} = (S_0/4)(1 - \alpha) \tag{13}$$

Equation (11) can be derived from Eq. (10) and (13) as follows.

$$\lambda_0 = -4 \times (S_0/4T_s)(1 - \alpha) = -(S_0/T_s)(1 - \alpha) = -1/\Lambda_0$$

$$\Lambda_0 = T_s/(1 - \alpha)S_0 \tag{11}$$

Based on the above analysis, whether Cess’s and Schlesinger’s calculations are correct or not depends on Eq. (9), assuming that  $\epsilon_{\text{eff}}$  is a constant.

According to the annual global mean energy budget [Kiehl et al., 1997], OLR can be expressed as follows.

$$\text{OLR} = F_{s,r} + F_{s,e} + F_{s,t} + F_{\text{sun}} - F_b \tag{14}$$

Here, $F_{s,r}$ :	surface radiation	390W/m <sup>2</sup>
$F_{s,e}$ :	surface evaporation	78W/m <sup>2</sup>
$F_{s,t}$ :	surface thermal conduction	24W/m <sup>2</sup>
$F_{\text{sun}}$ :	short waves absorbed by the atmosphere	67W/m <sup>2</sup>
$F_b$ :	back radiation	324W/m <sup>2</sup>
OLR:	outgoing long wave radiation	235W/m <sup>2</sup>

From Eq. (9) and (14), the following equations are obtained.

$$\epsilon_{\text{eff}}\sigma T_s^{**4} = \epsilon_{\text{eff}}F_{s,r} = F_{s,r} + F_{s,e} + F_{s,t} + F_{\text{sun}} - F_b \tag{15}$$

$$\epsilon_{\text{eff}} = 1 + (F_{s,e} + F_{s,t})/F_{s,r} + (F_{\text{sun}} - F_b)/F_{s,r} \tag{16}$$

Therefore,  $\epsilon_{\text{eff}}$  is not a constant but a complicated function of  $T_s$  and the internal variables  $I_j$ , which can not furnish the differentiation of Eq. (9) to obtain Eq. (10).

Based on the above arguments, we can conclude that Cess’s and Schlesinger’s calculations as well as that of Bony et al., can not be allowed as mathematically feasible in obtaining the genuine Planck feedback parameter.

**4.  $\lambda_0$  IN THE PRESENT STUDY**

From Eq. (8) and (14), the Planck feedback parameter  $\lambda_0$  is calculated by Eq. (17) referring to the linear model of the climate system expressed by Eq. (2).

$$\lambda_0 = -\partial\text{OLR}/\partial T_s = -d(F_{s,r} + F_{s,e} + F_{s,t})/dT_s - \partial(F_{\text{sun}} - F_b)/\partial I_j \times (dI_j/dT_s) \tag{17}$$

Here,  $I_j$  is the vector of the internal variables in the climate system.

Since the second terms are the climate feedback parameters of the internal variables  $I_j$ , they are zero when Planck feedback parameter  $\lambda_0$  is calculated. Thus, Eq. (17) is reduced to Eq. (18) utilizing the Stefan-Boltzmann Law.

$$\lambda_0 = -d(F_{s,r} + F_{s,e} + F_{s,t})/dT_s = -4(F_{s,r} + F_{s,e} + F_{s,t})/T_s \quad (18)$$

As shown above,  $F_{s,r} = 390\text{W/m}^2$ ;  $F_{s,e} = 78\text{W/m}^2$ ;  $F_{s,t} = 24\text{W/m}^2$   
Thus,  $\lambda_0$  can be calculated by Eq. (18) as follows.

$$\lambda_0 = -4 \times (390 + 78 + 24)/288 = -4 \times (390 + 102)/288 = -6.8(\text{W/m}^2)/\text{K}$$

Ramanathan obtained  $\Delta T_{s,0} = 0.50\text{K}$  with  $\Delta Q = 3.5\text{W/m}^2$  for the direct heating of  $\text{CO}_2$  doubling, which gives  $\Lambda_0 = 0.14\text{K}/(\text{W/m}^2)$  or  $\lambda_0 = -7.1(\text{W/m}^2)/\text{K}$  [Ramanathan, 1981]. In this study, the flux of evaporation  $F_{s,e}$  plus thermal conduction  $F_{s,t}$  is  $124\text{W/m}^2$ , when the radiation flux  $F_{s,r}$  is  $390\text{W/m}^2$ . Strictly speaking,  $(F_{s,e} + F_{s,t})$  is a different function of  $T_s$  from  $F_{s,r}$  as shown in Newell et al., for tropical seas [Newell et al., 1979]. However, the Stefan-Boltzmann Law is applied to  $(F_{s,r} + F_{s,e} + F_{s,t})$  in Eq. (18) as a first approximation [Ramanathan, 1981].

The following table shows a comparison between the present study and the data in the literature. Based on the argument presented in section 3, GROUP C is the theoretically relevant choice for  $T_s$  and OLR, while GROUP A and GROUP B can not be allowed on mathematic bases.

	$T_s$ K	OLR W/m <sub>2</sub>	$-\lambda_0$ (W/m <sup>2</sup> )/K	$\Lambda_0$ K/(W/m <sup>2</sup> )
(GROUP A)				
Cess, 1976	288	233	3.3	0.3
Schlesinger, 1986	288	*)	3.3	0.3
Wetherald et al., 1988	288	243**)	3.37	0.3
Cess et al., 1990	288	240	3.3	0.3
Tsushima et al., 2005	288	238**)	3.3	0.3
Soden et al., 2006	288	231**)	3.21***)	0.31***)
(GROUP B)				
Bony et al., 2006	255	242****)	3.8	0.26
(GROUP C)				
Ramanathan, 1981	288	390 + 124**)	7.1	0.14
Present study	288	390 + 102	6.8	0.15

\*) Solar constant  $S_0 = 1370\text{W/m}^2$  and surface albedo  $\alpha = 0.3$  in Eq. (11)

\*\*) Calculated by Eq. (10) with  $T_s = 288\text{K}$

\*\*\*) Averaged value of the 14 GCMs calculations for the IPCC AR4 [Soden et al., 2006]

\*\*\*\*) Calculated by Eq. (10) with  $T_s = 255\text{K}$

## 5. COMPARISON WITH THE IPCC AR4 AND OBSERVATIONAL DATA

Finally, the present study will be compared with the calculations of the 14 GCMs for the IPCC AR4 [Soden et al., 2006], in terms of  $\Delta T_{s,0}$  and  $\Delta T_s$  for  $\text{CO}_2$  doubling. The comparison will be made utilizing the averaged values of  $\lambda_{LR}$ ,  $\lambda_{WV}$ ,  $\lambda_A$  and  $\lambda_C$  from the IPCC AR4 [Soden et al., 2006].

	IPCC AR4 [Soden et al.,2006]	Present study
$\lambda_0$	$-3.21(\text{W}/\text{m}^2)/\text{K}$	$-6.8(\text{W}/\text{m}^2)/\text{K}$
$\lambda_{\text{LR}}$	$-0.84(\text{W}/\text{m}^2)/\text{K}$	$-0.84(\text{W}/\text{m}^2)/\text{K}$
$\lambda_{\text{WV}}$	$1.80(\text{W}/\text{m}^2)/\text{K}$	$1.80(\text{W}/\text{m}^2)/\text{K}$
$\lambda_{\text{A}}$	$0.26(\text{W}/\text{m}^2)/\text{K}$	$0.26(\text{W}/\text{m}^2)/\text{K}$
$\lambda_{\text{C}}$	$0.69(\text{W}/\text{m}^2)/\text{K}$	$0.69(\text{W}/\text{m}^2)/\text{K}$
$\Delta Q$	$3.7\text{W}/\text{m}^2$	$3.7\text{W}/\text{m}^2$
$\Delta T_{\text{s},0}$	$1.2\text{K}$	$0.54\text{K}$
$\Delta T_{\text{s}}$	$3.0\text{K}$	$0.75\text{K}$

Climate sensitivity  $\Delta T_{\text{s}}$  is 3K in the IPCC AR4, while it is 0.75K in the present study. A comparison will be made with observational data to investigate which value is more plausible.

- (1) According to the annual global mean energy budget [Kiehl et al., 1997], natural greenhouse energy can be expressed as  $(F_{\text{b}} - F_{\text{sun}})$  utilizing the same notation as Eq. (14), which furnishes a natural greenhouse effect of 33K. Therefore, the climate sensitivity  $\Delta T_{\text{s}}$  and its parameter  $\Lambda$  is calculated as follows utilizing the same radiative forcing  $\Delta Q$  of  $3.7\text{W}/\text{m}^2$  due to  $\text{CO}_2$  doubling as the IPCC AR4.

$$\Lambda = 33\text{K}/(F_{\text{b}} - F_{\text{sun}}) = 33\text{K}/(324 - 67)\text{W}/\text{m}^2 = 33\text{K}/257\text{W}/\text{m}^2 = 0.13\text{K}/(\text{W}/\text{m}^2)$$

$$\Delta T_{\text{s}} = 0.13\text{K}/(\text{W}/\text{m}^2) \times 3.7\text{W}/\text{m}^2 = 0.5\text{K}$$

Since climate change is a perturbation in the natural greenhouse effect due to  $\text{CO}_2$  doubling, this calculation is the most reliable method in evaluating climate sensitivity among the various observational methods.

- (2) From eight natural experiments, Idoso obtained  $\Delta T_{\text{s}} = 0.4\text{K}$  or less for  $\text{CO}_2$  doubling [Idoso, 1998]. Natural experiment 4 is substantially equivalent to method (1).
- (3) Based on data analysis from the Pinatubo event, Douglass et al., found that  $\Lambda$  is  $0.22\text{K}/(\text{W}/\text{m}^2)$ , which gives  $\Delta T_{\text{s}} = 0.8\text{K}$  with  $\Delta Q = 3.7\text{W}/\text{m}^2$  [Douglass et al., 2006].
- (4) Raval et al., obtained a sensitivity of  $0.3\text{K}/(\text{W}/\text{m}^2)$  or  $-3.3(\text{W}/\text{m}^2)/\text{K}$  for  $G_{\text{clear}} = \sigma T_{\text{s}}^{*4} - \text{OLR}_{\text{clear}}$  by ERBE measurements on the open ocean [Raval et al., 1989]. Utilizing the notation of Eq. (14),  $G_{\text{clear}}$  can be expressed as follows.

$$G_{\text{clear}} = F_{\text{s,r}} - (F_{\text{s,r}} + F_{\text{s,e}} + F_{\text{s,t}} + F_{\text{sun}} - F_{\text{b}}) = (F_{\text{b}} - F_{\text{sun}}) - (F_{\text{s,e}} + F_{\text{s,t}}) \quad (19)$$

Since  $(F_{\text{b}} - F_{\text{sun}})$  is the true greenhouse effect as shown in method (1),  $G_{\text{clear}}$  does not include the flux of surface evaporation and thermal conduction, which have a smaller range of sensitivity than radiation [Newell et al., 1979]. Furthermore, the relative humidity depends strongly on the large scale circulation which governs the distribution of water vapor with the strongest greenhouse effect [Held et al., 2000]. Therefore, it is to be concluded that the sensitivity obtained by Raval et al., is not the proper one to use in calculating the climate sensitivity  $\Delta T_{\text{s}}$ .

- (5) Gregory et al., obtained a climate sensitivity distribution curve having its maximum at 2K based on the sea temperature rise reported by Levitus et al. [Levitus et al., 2001; Gregory et al., 2002]. However, these results are not reliable since measurement problems exist in the data in Levitus et al. [Gouretski et al., 2007].

Based on the above argument, we concluded that the climate sensitivity  $\Delta T_s = 0.75\text{K}$  in the present study was good coincident with the observed values of  $0.4 - 0.8\text{K}$ . It is overestimated by the IPCC AR4 as  $\Delta T_s = 3\text{K}$  since the Planck feedback parameter  $\lambda_0$  is  $-3.21(\text{W}/\text{m}^2)/\text{K}$ , which is not mathematically feasible.  $\Delta T_s$  in the present study is  $0.25\text{K}$  larger than the  $0.5\text{K}$  obtained using method (1), which is the most reliable value. The discrepancy can be attributed to the overestimation of water vapor feedback in the IPCC AR4 [Minschwaner et al., 2004]. Furthermore, Lindzen proposed the possibility of negative water vapor feedback which diminishes climate sensitivity [Lindzen, 1990; Lindzen et al., 2001]. He also pointed out that the observed surface warming was far less than the calculated values using GCMs [Lindzen, 2007], which is in accordance with the present paper.

As to the overall effect of the various feedbacks, the following calculation shows that it is neutral or slightly negative .

$$\Delta T_s \text{ by method (1)}/\Delta T_{s,0} \text{ in the present study} = 0.50/0.54 = 0.93$$

This might be the cause of the stability in the present climate, though Earth's climate has experienced the Medieval Warm Period and the Little Ice Age due to fluctuations in solar activity.

## 6. CONCLUSION

The Planck feedback parameter  $\lambda_0$  is the most fundamental quantity in the theory of global warming, because the surface temperature change  $\Delta T_{s,0}$  is calculated by  $-(\text{radiative forcing due to CO}_2 \text{ doubling})/\lambda_0$  in the absence of feedbacks other than the changes in surface temperature. The following three groups of Planck feedback parameters are found in the literature depending on the choice of the temperature  $T_s$  and the outgoing long wave radiation (OLR) at the top of atmosphere in the equation of  $\lambda_0 = -4\text{OLR}/T_s$ , which is derived from the Stefan-Boltzmann Law.

$$\text{GROUP A: } T_s = 288\text{K and OLR} = 231\text{--}243\text{W}/\text{m}^2 \quad \lambda_0 = -3.21 - -3.37(\text{W}/\text{m}^2)/\text{K}$$

$$\text{GROUP B: } T_s = 255\text{K and OLR} = 242\text{W}/\text{m}^2, \quad \lambda_0 = -3.8(\text{W}/\text{m}^2)/\text{K}$$

$$\text{GROUP C: } T_s = 288\text{K and OLR} = 492\text{--}514\text{W}/\text{m}^2 \quad \lambda_0 = -6.8 - -7.1(\text{W}/\text{m}^2)/\text{K}$$

The present study shows that  $\lambda_0$  of GROUP C is the theoretically relevant choice for  $T_s$  and OLR rather than that of GROUP A or GROUP B, while the IPCC adopted  $\lambda_0$  of GROUP A. Although the surface temperature change  $\Delta T_s$  is  $3.0\text{K}$  with  $\lambda_0 = -3.21(\text{W}/\text{m}^2)/\text{K}$  for  $\text{CO}_2$  doubling when lapse rate, water vapor, surface albedo and cloud feedbacks are included in IPCC AR4, it is  $0.5 - 0.75\text{K}$  with  $\lambda_0 = -6.8(\text{W}/\text{m}^2)/\text{K}$  in the present study.

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